

Data-driven capacity estimation of commercial lithium-ion batteries from voltage relaxation

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Abstract:

Accurate capacity estimation is crucial for the reliable and safe operation of lithium-ion batteries. In particular, exploiting the relaxation voltage curve features could enable battery capacity estimation without additional cycling information. Here, we report the study of three datasets comprising 130 commercial lithium-ion cells cycled under various conditions to evaluate the capacity estimation approach. One dataset is collected for model building from batteries with $\text{LiNi}_{0.86}\text{Co}_{0.11}\text{Al}_{0.03}\text{O}_2$ -based positive electrodes. The other two datasets, used for validation, are obtained from batteries with $\text{LiNi}_{0.83}\text{Co}_{0.11}\text{Mn}_{0.07}\text{O}_2$ -based positive electrodes and batteries with the blend of $\text{Li}(\text{NiCoMn})\text{O}_2$ - $\text{Li}(\text{NiCoAl})\text{O}_2$ positive electrodes. Base models that use machine learning methods are employed to estimate the battery capacity using features derived from the relaxation voltage profiles. The best model achieves a root-mean-square error of 1.1% for the dataset used for the model building. A transfer learning model is then developed by adding a featured linear transformation to the base model. This extended model achieves a root-mean-square error of less than 1.7% on the datasets used for the model validation, indicating the successful applicability of the capacity estimation approach utilizing cell voltage relaxation.

Introduction

Lithium-ion batteries have become the dominant energy storage device for portable electric devices, electric vehicles (EVs), and many other applications¹. However, battery degradation is an important concern in the use of lithium-ion batteries as its performance decreases over time due to irreversible physical and chemical changes^{2,3}. State of Health (SoH) has been used as an indicator of the state of the battery and is usually expressed by the ratio of the relative residual capacity with respect to the initial capacity⁴. The accurate battery capacity estimation is challenging but critical to the reliable usage of the lithium-ion battery, i.e., accurate capacity estimation allows an accurate driving range prediction and accurate calculation of the maximum energy storage capability in a vehicle. Typically, the battery capacity is gained by a full discharge process after it has been fully charged. In a real-life usage scenario, the battery

45 full charge is often achieved while the EVs are parking with grid connection, however, the battery
46 discharge depends on the user behavior with uncertainties in environmental and operational conditions, a
47 complete discharge curve is seldom available for on-board battery health monitoring. The battery charging
48 and discharging voltage, as one of the easily obtained parameters, depend on both, thermodynamic and
49 kinetic characteristics of the battery. Thus, those methods using a charge/discharge process are proposed to
50 estimate capacity for practical applications^{5,6}, in which the input variables are extracted from the measured
51 voltage curves, and the data-driven methods using statistical and machine learning techniques have been
52 popular in battery research recently due to their strong data processing and nonlinear fitting capabilities^{7,8}.
53 The data-driven methods do not need a deep understanding of battery electrochemical principles, but large
54 numbers of data are required to ensure the reliability of model⁹. Severson et al.¹⁰ reported a promising route
55 using machine learning to construct models that accurately predicted graphite||LiFePO₄ (LFP) commercial
56 cell lives using charge-discharge voltage data. Zhang et al.¹¹ identified battery degradation patterns from
57 impedance spectroscopy using Gaussian process machine learning models. Ding et al.¹² introduced a
58 machine learning method for the improvement of the efficiency of membrane electrode assembly design
59 and experiment. Such data-driven methods focus on the relationships among the input and output features,
60 and a key part of data-driven battery state estimation is the extraction of degradation features, which largely
61 determines the estimation performance¹³⁻¹⁵.

62 In practical electric transport applications, battery charging is essential and happens regularly
63 compared to the random discharge process affected by the driving behaviors and road environments.
64 Therefore, extracting voltage features from the charging process has attracted wide attention. Taking into
65 account the state-of-the-art literature, three classes of voltage-based extraction methods can be defined: (I)
66 CC (constant current) charge voltage-based, (II) CC-CV (constant current-constant voltage) charge
67 voltage-based, and (III) rest voltage-based as listed in Supplementary Table 1. The partial charge process
68 in a specific voltage range for feature extraction is commonly used for capacity estimation¹⁶, and the
69 estimation accuracy of the state of art is ranging from a root-mean-square error (RMSE) of 0.39% to a
70 RMSE of 4.26% based on in-house experiments and different public datasets^{5,6,17}. The transformations of
71 the partial voltage curves, i.e., differential voltage analysis^{18,19} and incremental capacity analysis²⁰⁻²², are
72 used for battery aging mechanism identification and capacity fade evaluation. Typically, SVR (Support
73 Vectors Regression)²³, GPPF (Gaussian Process Particle Filter)²⁴, BPNN (Back-Propagation Neural
74 Network)²⁵, and linear model²⁶ are applied to estimate battery capacity using the partial incremental
75 capacity curve. Compared to the charge voltage-based methods, studies extracting features from the rest
76 voltage are few. A representative battery capacity estimation method utilizing the resting process was
77 proposed by Baghdadi et al.²⁷. They proposed a linear model to estimate battery capacity using the
78 voltage after 30 min rest when the cell is fully charged, and the capacity estimation percentage error is
79 ranging from 0.7% to 3.3% for three different commercial batteries. Schindler et al.²⁸ and C. Lüders et al.
80²⁹ took the voltage relaxation for the lithium plating detection in the battery capacity fade process. Qian et
81 al.³⁰ used an equivalent circuit model (ECM) to describe the voltage relaxation and found that the
82 extracted parameters provided an evaluation of the battery SoH and aging mechanisms. Attidekou et al.³¹
83 modeled the battery capacity decay during rest periods at 100% SoC using a dynamic time constant
84 derived from the resistor-capacitor (RC) network model. However, as the amount of RC links increases,
85 the complexity of the ECM will increase accordingly, which makes it difficult to use in an on-board
86 application³². Besides, the accuracy and robustness of capacity estimation are difficult to evaluate
87 because of the differences in battery types and working conditions^{9,10}.

88 It has been proven that the relaxation process including the relaxation voltage value at a specific time
89 and the voltage curve during a specific period shows a relationship with the battery SoH^{28-31,33}. From the
90 review of battery charging studies³⁴⁻³⁶, the real-time data of EVs^{37,38}, and a survey of real-world EV

91 charging (Supplementary Note 1, Supplementary Table 2 and 3, and Supplementary Figure 1 and 2), in
92 addition to the CC charging strategy, the multistage current charging algorithm using a SoC dependent
93 charging current is a promising method to maximize the charging efficiency. The start of charge for the
94 EVs is normally distributed around intermediate SoCs as expected from the statistics^{37,39,40}. The various
95 multistage current charge strategies and the uncertain start of charge points bring difficulties to the
96 acquirement of specific voltage ranges under constant current in the voltage-based methods. The
97 relaxation after being fully charged is relatively unaffected by the charging process and is also easy to
98 obtain since the battery is fully charged with high probability in real EV usage^{37,39,40}, there is also no
99 need for additional devices as the voltage data can be directly obtained from the battery management
100 system. However, to the best of our knowledge, the relaxation voltage curve of the battery has not yet
101 been studied systematically with machine learning methods for large-scale data from different battery
102 types. Herein, an approach based on features extracted from the battery relaxation voltage is proposed,
103 which focuses on short-term battery capacity estimation without any previous cycling information for
104 on-board implementation.

105 In this study, base models using machine learning methods, i.e., the linear model (ElasticNet⁴¹), and
106 nonlinear models (XGBoost⁴² and Support Vector Regression (SVR)⁴³), using large datasets from three
107 kinds of commercial lithium-ion batteries are employed. The model inputs are statistical features
108 extracted from the voltage relaxation curve. Batteries with $\text{LiNi}_{0.86}\text{Co}_{0.11}\text{Al}_{0.03}\text{O}_2$ positive electrode (NCA
109 battery) cycled at different temperatures and current rates are used for base model building, showing the
110 best test performance with a RMSE of 1.0%. The transfer learning method is applied on batteries with
111 $\text{LiNi}_{0.83}\text{Co}_{0.11}\text{Mn}_{0.07}\text{O}_2$ positive electrode (NCM battery) and batteries with 42 (3) wt.% $\text{Li}(\text{NiCoMn})\text{O}_2$
112 blended with 58 (3) wt.% $\text{Li}(\text{NiCoAl})\text{O}_2$ positive electrode (NCM+NCA battery), obtaining 1.7% RMSE
113 and 1.6% RMSE respectively, and enabling the generalizability of our approach.

114 **Results**

115 **Data generation**

116 Large cycling datasets on NCA battery, NCM battery, and NCM+NCA battery are created in this
117 study. The batteries are cycled in a temperature-controlled chamber with different charge current rates.
118 The battery specifications are listed in Supplementary Table 4. Long-term cycling is conducted on all
119 cells with a summary of cycling conditions in Table 1. The temperatures chosen are 25 °C, 35 °C, and
120 45 °C. Current rates ranging from 0.25 C (0.875 A) to 4 C (10 A) are used. The current rate is calculated
121 from the nominal capacity of batteries, i.e., 1C is equal to 3.5 A for the NCA battery and NCM battery,
122 and 1C is equal to 2.5 A for the NCM+NCA battery. The cells are named as CYX-Y/Z according to their
123 cycling conditions. X means the temperature, Y/Z represents the charge/discharge current rate. The
124 number of cells assigned to each cycling condition in Table 1 is aimed to obtain a dataset covering
125 possible variations between cells. One data unit comprises a relaxation voltage curve after full charge
126 with the following discharge capacity. Each relaxation voltage curve is transformed into six statistical
127 features, i.e., variance (Var), skewness (Ske), maxima (Max), minima (Min), mean (Mean), and excess
128 kurtosis (Kur). The mathematical description of the six features is depicted in Supplementary Table 5. The
129 datasets collected from NCA, NCM, and NCM+NCA cells are named as dataset 1, dataset 2, and dataset
130 3 in this study, respectively. Dataset 1 is used for base model training and test. Dataset 2 and dataset 3 are
131 used for assessing and improving the generalizability of the proposed approach by transfer learning.

132 Voltage and current are the basic data recorded in these experiments, which include charging,
133 discharging, and relaxation processes. The cell cycling is performed with constant current (CC) charging
134 to 4.2 V with current rates ranging from 0.25 C (0.875 A) to 1 C (3.5 A), followed by a constant voltage

(CV) charging step at 4.2 V until a current of 0.05 C is reached. Constant current is then employed for the discharge to 2.65 V for the NCA cells and 2.5 V for the NCM and NCM+NCA cells, respectively. One complete cycling curve using a 0.5 C charging rate for the NCA cell is shown in Figure 1a, which includes five processes, i.e., (I) CC charging, (II) CV charging, (III) relaxation after charging, (IV) CC discharging, and (V) relaxation after discharging. The CC discharging capacity is treated as the battery residual capacity during cycling. The relaxation time between the CV charging and CC discharging is 30 minutes for the NCA battery and NCM battery with a real sampling time of 120 s, and it is 60 minutes for the NCM+NCA battery with a sampling time of 30 s. The starting and ending voltage during the battery relaxation show a declining trend with increasing cycle number as presented in Figure 1b.

Three datasets with capacity down to 71% of the nominal capacity are generated. The battery capacity as a function of cycle number for the NCA cells is shown in Figure 1c. The cycle number is ranging from 50 to 800 in the 100% - 71% capacity window. It is evident that both, charging current and temperature have a strong influence on the capacity decay, and the battery capacity shows significant variance as depicted in the embedded plot in Figure 1c, indicating the degradation distribution of the cycled cells. The worst scenario is the one with cells cycled at 1C charge at 25 °C (CY25-1/1), only 50 cycles can be obtained until the cells reach 71% of the nominal capacity. 71% capacity is reached after 125 and 600 cycles at 25 °C and 35 °C respectively, for cells charged with 0.5 C (CY25-0.5/1, and CY35-0.5/1). 71% capacity is reached after 250 cycles at 25 °C with 0.25 C charging current (CY25-0.25/1) and in a range of 500 to 800 cycles at 45 °C with 0.5C charging current (CY45-0.5/1). The cycling data of the NCM cells are shown in Figure 1d. Fatigue down to 71% residual capacity is found between 250 and 500 cycles (25 °C), 1250 and 1500 cycles (35 °C), and around 1000 cycles at 45 °C cycling temperature. The capacity fade results indicate that increasing the temperature to 35 °C and 45 °C has a beneficial effect on the capacity retention and that the charging current is at the limit of what the cells can handle. For NCA and NCM cells, a capacity spread for the cells cycled under equal conditions is observed, which is speculated to be ascribed to the intrinsic manufacturing variations as this spread is already seen at the beginning of cycling^{44,45}. The cycling data of the NCM+NCA cells are shown in Figure 1e, exhibiting a linear degradation trend regardless of the cycling discharge rates, and 71% residual capacity appears in a range of 750 to 850 cycles showing the influence of the cell cycling conditions.

Feature extraction

Summarizing statistics are proven to be effective to illustrate numerically the shape and position change of the voltage curve^{5,10}. As mentioned above, the relaxation process after fully charging is taken for feature extraction because of its strong relationship with battery degradation and its easy acquisition in battery real use. Each voltage relaxation curve is converted to six statistical features, i.e., Var, Ske, Max, Min, Mean, and Kur, as displayed in Figure 2.

The relationship between battery capacity and the corresponding features is dependent on the cycling conditions as presented in Figure 2. It can be seen that it is difficult to describe the relationships only by linear functions. The Var in Figure 2a represents the distribution of the voltage points in one relaxation process, a decrease of Var versus capacity fade means that the relaxation voltages show a sharper distribution with increasing cycle number, and vice versa. Both Ske and Kur are normalized using Var, they are used to describe the shape of the corresponding voltage curve. The Ske in Figure 2b is positive for almost all cycling conditions, indicating that more than half of the sampled voltage data are below the average voltage (Mean), which corresponds to the shape of the relaxation voltage curve, i.e., with respect to the relaxation time, the voltage drops initially fast and then gradually slows down. The Max in Figure

179 2c presents a monotonous decrease of the maximum voltage versus capacity drop for all cycling
180 conditions. The Min and Mean first increase and then decrease versus the capacity reduction as displayed
181 in Figure 2d and Figure 2e, respectively. The Kur shown in Figure 2f is the excess kurtosis obtained from
182 the kurtosis of the raw data minus the kurtosis of a normal distribution. The excess kurtosis is negative for
183 all cycling conditions, meaning that the distribution of the relaxation voltage is gentler than a normal
184 distribution.

185 **Capacity estimation**

186 Based on the features extracted from the relaxation voltage curve after charging, data-driven
187 methods are used for battery capacity estimation. Owing to the difference in the order of magnitudes of
188 the features, a standard normalization for battery features is performed for dataset 1. The features of
189 dataset 2 and dataset 3 are normalized by applying the same normalizing scales as used for dataset 1. The
190 capacity is uniformized considering the difference in the battery nominal capacity. The XGBoost⁴² is
191 selected as the main machine learning method. The ElasticNet⁴¹ as the multivariate linear model is used
192 for comparison, and the SVR⁴³ is a support for the verification of the transfer learning approach. For the
193 base model training and test, different data splitting strategies are compared with dataset 1 in
194 Supplementary Note 2 and Supplementary Table 6-9. The best test result of the temperature dependence
195 splitting method shows a 1.5% RMSE. A 2.3% test RMSE is obtained from the time-series data splitting
196 method. The data random splitting and cell stratified sampling methods achieve good estimation accuracy
197 with 1.1% RMSEs, implying that the variation of the working conditions leading to different degradation
198 patterns is essential to improve the generalization of the model. The results of cell stratified sampling
199 method meaning that the data from the same cell is either in the training set or in the test set are presented
200 in this study (Strategy D in Supplementary Note 2). The cells are approximately in a 4:1 ratio for training
201 and test (Supplementary Table 9). In the model training process, the K-fold cross-validation with K=5 is
202 used to determine the hyperparameters of the models. A feature reduction is performed by using different
203 feature combinations to reduce the number of inputs and simplify the model complexity. The
204 cross-validation RMSEs under different feature combinations using the XGBoost method are compared in
205 Figure 3. The *i* and *j* are used to represent different feature combinations referring the Supplementary
206 Table 10.

207 It shows that the RMSE gradually decreases as the number of features increases, and the accuracy
208 improvement is no longer obvious after using three features in Figure 3. The best estimation result is
209 obtained by the input [Var, Ske, Max] in a three feature combination. The effect of the duration of the
210 relaxation on the capacity estimation is presented in Supplementary Figure 3, in which the RMSEs of
211 training and test decrease as the relaxation time increases in the XGBoost method, indicating that longer
212 relaxation time improves the model accuracy. Therefore, the Var, Ske, and Max of the voltage relaxation
213 after 30 minutes are extracted as inputs for the base model. The hyperparameters of each algorithm are
214 available in Supplementary Table 11. The RMSEs of different estimation methods on dataset 1 are
215 summarized in Figure 4a. It can be concluded that the test RMSE of XGBoost and SVR all reaches 1.1%,
216 showing better performance than the linear model, and the RMSEs of train and test are close to each other,
217 indicating the effectiveness of data splitting. The estimated capacity versus real capacity is illustrated in
218 Figure 4b-4d for visualization purposes.

219 **Performance of the proposed approach**

220 The performance of the proposed approach is benchmarked with state-of-the-art models using
221 voltage curves for battery capacity estimation as shown in Table 2. One representative method is selected
222 from each class of the presented capacity estimation methods (Supplementary Table 1). Since the datasets

223 used in the literature are different in battery material and test procedures from ours, the strategy to solve
224 this difference is to apply their algorithms to our datasets. A detailed description of data processing and
225 estimation results for each method is presented in Supplementary Note 3 and Supplementary Figure 4-7.
226 The performance of the linear model to estimate the battery capacity based on the resting voltage in Ref.
227 ²⁷ shows a 2.5% RMSE, which can be explained by the large data volume and variety of working
228 conditions in our dataset 1 highlighting the difficulty of capacity estimation only with the linear model. In
229 the CC charge voltage-based methods, the random forest regression (RFR) method ¹⁷ using the voltage
230 ranging from 3.6V to 3.8 V achieves a RMSE of 1.0% on dataset 1, which is 0.1% less than our RMSE
231 based on the voltage relaxation. A method based on the remaining electrical charge with a threshold
232 according to the incremental capacity value is proposed in Ref. ²⁶. The application of the same
233 incremental capacity transformation method on dataset 1 provides a RMSE of 1.3%, indicating that our
234 proposed approach has better accuracy. The Gaussian process regression (GPR) method ⁴⁶ using a full
235 CC-CV charge voltage curve obtains good estimation results on dataset 1 with a test RMSE of 1.1%.
236 Compared with the current research status, especially with respect to large datasets, the proposed
237 approach using resting voltage can achieve a good estimation accuracy. As mentioned in the introduction
238 section, there are some challenges in the acquisition of specific charging voltage curves because the start
239 of battery charge is usually dependent on the driver behavior and the charge modes differ significantly
240 from the charging stations in the real application of EVs. The relaxation process of a battery being fully
241 charged is easily obtained without the requirement of specific working conditions and voltage ranges,
242 which offers a new sight for battery capacity estimation.

243 **Physical explanation**

244 The alternating current (AC) electrochemical impedance provides information in the frequency
245 domain on the degradation mechanisms of the battery as proven in Ref.⁴⁷. The degradation mechanisms
246 can be determined from the change of electrochemical impedance parameters extracted by fitting the
247 impedance spectra with an ECM ⁴⁸. A schematic plot of electrochemical impedance spectra during cycling
248 and the corresponding ECM are complemented in Supplementary Figure 8. Basically, an increase of R0 is
249 likely due to contact loss and the reduction of ionic conductivity in the electrolyte ⁴⁹. R1 represents the
250 resistance associated with the anode solid electrolyte interphase (SEI) indicated by the semicircle at high
251 frequencies ⁴⁸. R2 is the charge-transfer resistance describing the rate of electrochemical reaction, which
252 is related to the loss of electrode material through particle cracking ^{19,50}. The capacity loss of the cycled
253 cells in dataset 1 and dataset 2 has been investigated by in situ neutron powder diffraction in our previous
254 work ⁴⁴, which exhibits that the decrease in lithium content in the positive and negative electrodes
255 correlates well with the observed discharge capacity. Both positive and negative electrodes do not
256 decompose to other crystalline phases during cycling, but the lithium loss in the electrodes leading to
257 lithiated material loss is traced by detecting changes in the lattices of the electrodes. The lithiated material
258 loss and the SEI formation are suspected to contribute to the lithium loss.

259 Herein, the dominating aging factors for each cycling group are discussed by fitted electrochemical
260 impedance parameters in Figure 5. The coefficient of determination (R^2) of each measured impedance
261 spectrum between the raw and fitted data is summarized in Supplementary Table 12. All R^2 values are
262 greater than 0.999, indicating the credible fitting accuracy. All the raw and fitted impedance data can be
263 found from the data availability. By comparison of the resistance increment from the initial value (R_{init})
264 for all three type cells, the increment of R0 is minimal (Figure 5a, 5b, and 5c), followed by R1 (Figure 5d,
265 5e, and 5f). R2 shows the highest increase during the battery capacity fade as shown in Figure 5g, 5h, and
266 5i. The dominating degradation factors are different under different working conditions. For the NCA cell,

267 as shown in Figure 5a, the CY25-0.25/1 shows a steady and relatively small increase of R0, nevertheless,
268 its R1 in Figure 5d shows an accelerated rise, indicating the increase in the thickness of the SEI layer. The
269 R2 of CY25-0.25/1 in Figure 5g presents a similar increasing trend to its R0. The R0 of CY25-0.5/1 and
270 CY25-1/1 in Figure 5a remains the largest resistive contribution throughout, but their R1 and R2 are
271 relatively lower than that of others, which indicates a more serious cell degradation such as electrolyte
272 dry-out or contact loss likely caused by lithium plating^{49,51}. For the results of NCM cells in Figure 5b, 5e,
273 and 5h, all resistances of CY25-0.5/1 increase slowly, while resistances of cells cycled at 35°C and 45 °C
274 exhibit a large increase rate. For the NCA+NCM cells, the influence of discharge rate is mainly
275 represented by R1 by comparing the results in Figure 5c, 5f, and 5i. The CY25-0.5/4 SEI resistance
276 increase in Figure 5f is significantly slower than that of other cycling conditions. The temperature
277 influence on the degradation mechanism can be seen in Figure 5g and Figure 5h, in which the increase of
278 R2 is associated mainly with the increase of ambient temperature. The cells cycled at 45°C and 35 °C
279 mainly lead to an increase of R2, which could be associated with the positive active material loss, e.g.,
280 particle cracking and pulverization^{52,53}. The diversity of the battery internal degradation mechanisms
281 results in various degradation paths, which can explain the difficulty in applying a simple linear model on
282 the battery capacity estimation. Additionally, it seems that different battery types follow to some extent
283 similar degradation rules, e.g., the exponential rise of R2, inspiring the use of transfer learning in the
284 following part.

285 **Approach verification by transfer learning**

286 The transfer learning (TL) method, which is applied to improve the learning ability by rebuilding the
287 machine learning model using a relatively small amount of newly collected data, is proposed for easy
288 adaption to the variation of voltage features existing in dataset 2 and dataset 3 in which different batteries
289 and cycling conditions are used. The model weights are pre-trained through dataset 1 to obtain the base
290 model. Then, some new data units from dataset 2 and dataset 3 are set as the input variable to re-train the
291 TL model. Different data selection methods are discussed in Supplementary Note 4 and Supplementary
292 Table 13, depicting that the variation of working conditions is necessary to improve the accuracy of the
293 model estimation. One cell is randomly selected from each cycling condition in dataset 2 and dataset 3,
294 then the data units in each cell are chosen with an interval of 100 cycles as the input variables for the
295 re-training of TL models (Strategy D in Supplementary Note 4). The sizes of the input variable are
296 summarized in Supplementary Table 14 (occupying 0.06% of dataset 2 and 0.35% of dataset 3).
297 Verification on dataset 2 and dataset 3 without changing any weights of the base model is used as a
298 zero-shot learning (ZSL) reference. The full base model is retrained using the same input variables from
299 dataset 2 and dataset 3 as a No TL comparison. Two TL methods (TL1 and TL2) with fine-tuning
300 strategies are activated to adjust the weights of a newly added layer, while the weights of other layers
301 remain unchanged. TL1 means that a linear transformation layer is added before the output of capacity.
302 TL2 means that a linear transformation layer before the base model is constructed to adapt the input
303 features as illustrated in Supplementary Figure 9. The test RMSEs are compared in Table 3.

304 The ZSL strategy obtains more than 3.4% test RMSE on all datasets directly using the base models.
305 The error between the estimated capacity and real capacity is quite large as shown in Supplementary
306 Figure 10, meaning that the differences in battery types and materials cannot be ignored. When the base
307 model is retrained in the No TL strategy, the XGBoost reaches a 2.9% test RMSE on dataset 2 and a 2.0%
308 test RMSE on dataset 3, and the SVR gives no obvious improvement in the accuracy (Supplementary
309 Figure 11 and Supplementary Table 15). When the TL1 is applied on dataset 2 and dataset 3, the test
310 RMSE of the SVR method goes down to 2.6% and 3.5% respectively, but a high number of outliers still

311 appears in Supplementary Figure 12. The results of estimated capacity versus real capacity by TL2 are
312 presented in Figure 6. The test RMSE is reduced to 2.4% by the XGBoost using the TL2 on dataset 2,
313 noting that the performance of XGBoost using the No TL on dataset 3 is better than that of TL, which
314 could be ascribed to the narrow distribution of capacity fade in dataset 3. The best accuracies on dataset 2
315 and dataset 3 are all reached by SVR using the TL2, showing test RMSEs of 1.7% and 1.6%, respectively.
316 It can be concluded that the use of TL2 improves the estimation accuracy, and the reason behind the
317 accuracy improvement is that a linear transformation of the input features helps the model adapt to the
318 differences in battery types but similarity degradation modes. Interestingly, we find that the SVR is more
319 reliable and suitable for transfer learning than the XGBoost with a small amount of newly collected data.
320 The possible reason is that the XGBoost is a discrete gradient boosting framework, the output of the
321 model is limited by the base model even if a new layer is added before the base model, whereas the SVR
322 is a kernel-based framework, in which the continuous calculation achieves a better prediction under the
323 designed TL2. In summary, the proposed approach using the relaxation voltage curve is useful to estimate
324 the battery capacity, and the transfer learning improves the accuracy of capacity estimation requiring little
325 tuning to adapt to the difference in batteries.

326 **Discussion**

327 Accurate identification of lithium-ion battery capacity facilitates the accurate estimation of the
328 driving range which is a primary concern for EVs. An approach without requiring information from the
329 previous cycling to estimate battery capacity is proposed. The proposed approach uses three statistical
330 features ([Var, Ske, Max]) extracted from the voltage relaxation curve as input to predict the capacity in
331 the next cycle. The transfer learning embedding machine learning methods is applied on 130 cells to
332 establish a suitable model and for the verification of the approach. The best base model achieves a
333 root-mean-square error of 1.1%. The transfer learning adding a linear transformation layer before the base
334 model shows good predictive ability within a RMSE of 1.7% on different batteries. The retraining of
335 transfer learning only needs a small number of data units on the condition that a variation of the input data
336 needs to be guaranteed to improve the applicability of the proposed approach. The relaxation process of a
337 battery after full charge is easily obtained without the requirement of specific working conditions and
338 voltage ranges, providing a new possibility for battery capacity estimation using data-driven methods in
339 the system implementation of EV applications.

340 **Methods**

341 **Cell selection and cycling**

342 Commercially available lithium-ion batteries, i.e., LG INR18650-35E (3.5 Ah, 3.6 V), Samsung
343 INR18650-MJ1 (3.5 Ah, 3.6 V), and Samsung INR18650-25R (2.5Ah, 3.6 V), have been tested. More
344 battery specifications are listed in Supplementary Table 4. The positive electrode compositions of the
345 INR18650-35E battery and INR18650-MJ1 battery are $\text{LiNi}_{0.86}\text{Co}_{0.11}\text{Al}_{0.03}\text{O}_2$ and $\text{Li}(\text{Ni}_{0.83}\text{Co}_{0.11}\text{Mn}_{0.07})\text{O}_2$
346 respectively, and the negative electrodes for both cell types have roughly 97 wt% C and 2 wt% Si as well
347 as traces of H, N, and S from Ref. ⁴⁴. The positive electrode of the INR18650-25R battery is the blend of
348 42 (3) wt.% $\text{Li}(\text{NiCoMn})\text{O}_2$ - 58 (3) wt.% $\text{Li}(\text{NiCoAl})\text{O}_2$, and the negative electrode is graphite from Ref.
349 ¹⁹. The INR18650-35E battery is named as NCA battery. The INR18650-MJ1 is named as NCM battery.
350 The INR18650-25R is named as NCM+NCA battery according to the positive electrode. A potentiostat
351 (BioLogic BCS-815, France) is employed for cell cycling. The measurements are conducted at 25 °C, 35
352 °C, and 45 °C in a climate chamber (BINDER, ± 0.2 °C, Germany). Long-term cycling is conducted on a
353 total of 130 cells with a summary of cycling conditions as provided in Table 1. A schematic connection of

354 the potentiostat, chamber, and cells is shown in Supplementary Figure 13. For the NCA and NCM
 355 batteries, the metal taps are spot-welded to the cells, and the contact is soldered to the metal taps. A
 356 four-wire holder is used for the NCM+NCA battery. For partially charged/discharged NCA and NCM
 357 cells, the electrochemical impedance is measured in the fully charged state using a frequency range of 10
 358 kHz to 50 mHz (20 data points per decade of frequency) and a potential amplitude of 20 mV. 30 minutes
 359 are set at the open circuit voltage before the electrochemical impedance tests. The electrochemical
 360 impedance is tested every 25 cycles for the NCA battery and every 50 cycles for the NCM battery. For the
 361 NCM+NCA battery, the electrochemical impedance is conducted every 50 cycles at full charge in a range
 362 of 10 kHz to 0.01 Hz (6 data points per decade of frequency) with a sinusoidal amplitude of 250 mA. 60
 363 minutes are set at the open circuit voltage before the electrochemical impedance tests. The NCA cells and
 364 NCM cells are tested from 2016 to 2018, and the NCM+NCA cells are cycled in 2020. Different
 365 experimenters at different test periods are responsible for the difference in battery connection methods
 366 and experimental parameters in AC impedance tests, e.g., perturbation modes, perturbation amplitudes,
 367 and open circuit voltage time.

368 **Machine learning methods**

369 Two transfer learning strategies embedding the XGBoost method and SVR method are applied in our
 370 study, and an illustration of the implemented transfer learning process is shown in Supplementary Figure
 371 9. The algorithms of the ElasticNet method, XGBoost method, and SVR method are introduced in
 372 Supplementary Note 5.

- 373 1) The base model is trained on all experimental data of NCA batteries (dataset 1). Firstly, the base
 374 model is directly verified on dataset 2 and dataset 3 without changing model weights as a zero-shot
 375 learning (ZSL) reference.
- 376 2) The base model is retrained using some new data units (Strategy D in Supplementary Note 4) as input
 377 variables from dataset 2 and dataset 3 as a No TL comparison.
- 378 3) Two transfer learning strategies (TL1 and TL2) are proposed by adding layers behind and in front of
 379 the base model. All weights in the base model are frozen in the transfer learning strategies except the
 380 newly added layer. In detail, TL1 means that a linear transformation layer is added before the output of
 381 capacity, which is described as

$$382 \quad Q' = wQ + b \quad (1)$$

383 TL2 means that a linear transformation layer is constructed to adapt the input features, which is described
 384 as

$$385 \quad \begin{bmatrix} \text{Var}' \\ \text{Ske}' \\ \text{Max}' \end{bmatrix} = W \begin{bmatrix} \text{Var} \\ \text{Ske} \\ \text{Max} \end{bmatrix} + b \quad (2)$$

386 w , W , and b are the weights in the added layer. The target dataset from dataset 2 and dataset 3 are selected
 387 to train the new layer weights.

- 388 4) The transfer learning models are verified on the remaining dataset 2 and dataset 3 respectively. The
 389 test RMSEs are compared in Table 3, and the estimation results are presented in Figure 6 and
 390 Supplementary Figure 10-12 for visualization purposes.

391 **Data availability**

392 The data generated in this study have been deposited in the Zenodo database under accession code
 393 [<https://doi.org/10.5281/zenodo.6379165>].

394 **Code availability**

395 The data processing is performed in python and is available at
396 [<https://github.com/Yixiu-Wang/data-driven-capacity-estimation-from-voltage-relaxation>]. Code for the
397 modelling work is available from the corresponding authors upon request.

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517 **Author Contributions**

518 Conceptualization, writing, and original draft preparation were done by J.Z., Y.W., and H.D. The
519 experimental studies were performed by J.Z., L.M., M.J.M., and M.H. The computational studies are
520 performed by Y.W., J.Z., and Y.H. R.B.G., Y.C., X.L., H.D., M.K., M.H., A.S., and H.E. were involved in
521 the writing, review, and editing of this manuscript. H.D., M.K., X.W., and H.E. supervised the work.

522 **Competing interests**

523 The authors declare no competing interests.

524

525 Table 1 Cycled batteries and cycling conditions for the dataset generation. All cells are commercial 18650
 526 type batteries. The cycling temperature is controlled by climate chambers (± 0.2 °C). The current rate is
 527 calculated from the battery nominal capacity (1C =3.5 A for the NCA battery and NCM battery, and
 528 1C=2.5 A for the NCM+NCA battery).

datasets	Cell type	Cycling temperature (± 0.2 °C)	Charge current rate (C)/discharge rate (C)	Number of cells	Number of data units
Dataset 1	NCA battery Type: 18650 Cutoff Voltage: 2.65 - 4.2V Nominal capacity: 3.5 Ah	25	0.25/1	7	1853
			0.5/1	19	3278
			1/1	9	260
		35	0.5/1	3	1112
		45		28	15775
Dataset 2	NCM battery Type: 18650 Cutoff Voltage: 2.5 - 4.2V Nominal capacity: 3.5 Ah	25	0.5/1	23	5490
		35		4	4712
		45		28	17600
Dataset 3	NCM+NCA battery Type: 18650 Cutoff Voltage: 2.5 - 4.2V Nominal capacity: 2.5 Ah	25	0.5/1	3	2843
			0.5/2	3	2913
			0.5/4	3	2826

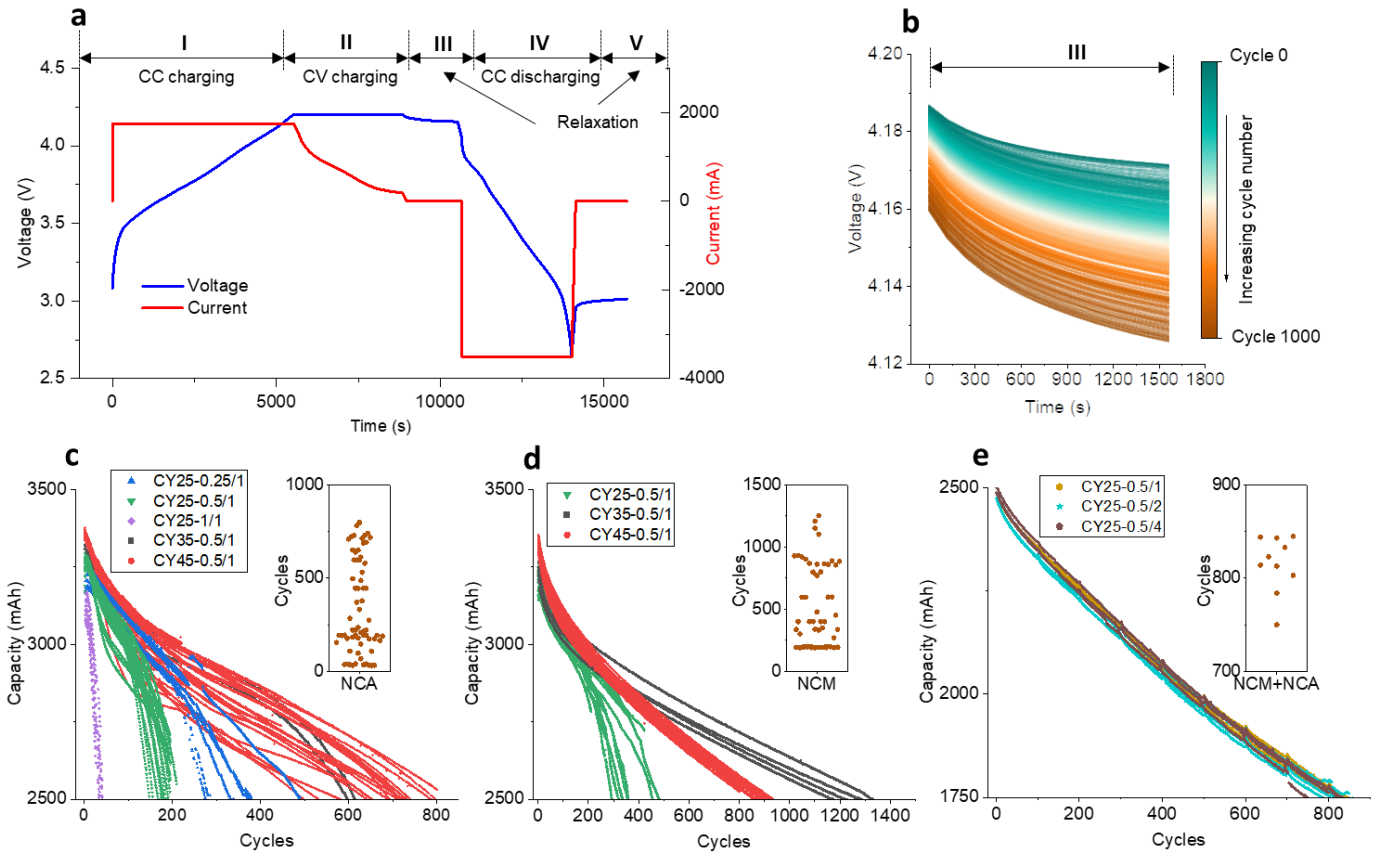
529
 530 Table 2 Test means root-mean-square error (RMSE) of different models using voltage-based features for
 531 battery capacity estimation

Features from	Methods	Test RMSE on Dataset 1
Rest voltage-based	Linear model ²⁷	0.025
Constant current charge voltage-based	Random forest regression ¹⁷	0.010
Incremental capacity analysis transformation	Linear model ²⁶	0.013
Constant current - constant voltage charge voltage-based	Gaussian process regression ⁴⁶	0.011

532
 533 Table 3 Test RMSEs of battery capacity estimation using zero-shot learning (ZSL) and different transfer
 534 learning (TL) methods on dataset 2 and dataset 3

Methods	Dataset	ZSL	No TL	TL1	TL2
XGBoost	Dataset 2	0.038	0.029	0.027	0.024
	Dataset 3	0.038	0.020	0.034	0.024
Support Vectors Regression	Dataset 2	0.034	0.039	0.026	0.017
	Dataset 3	0.073	0.052	0.035	0.016

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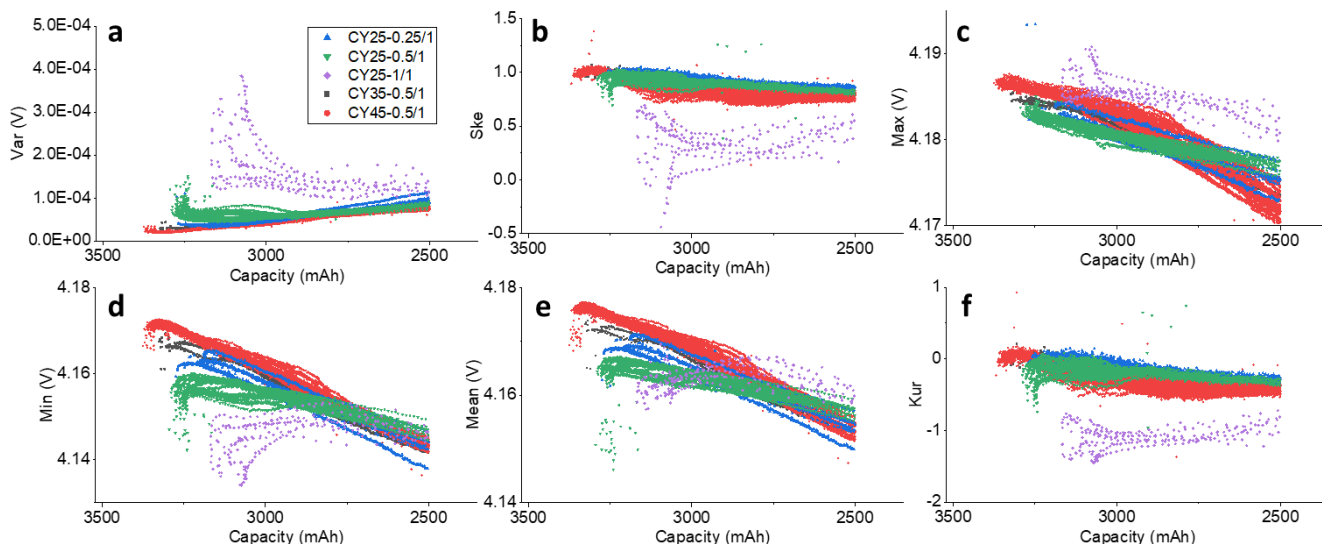
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Figure 1 Battery cycling data. Voltage and current profile in the first cycle of one CY25-0.5/1 NCA battery (a). A plot of relaxation voltage change (region III) while cycling for one NCA cell (b). NCA battery discharge capacity (until 71% of nominal capacity) versus cycle number of NCA battery (c), NCM battery (d), and NCM+NCA battery (e). The embedded plots in c, d, and e are the cycle distribution of cells at around 71% of nominal capacity, the points are offset randomly in the horizontal direction to avoid overlapping.



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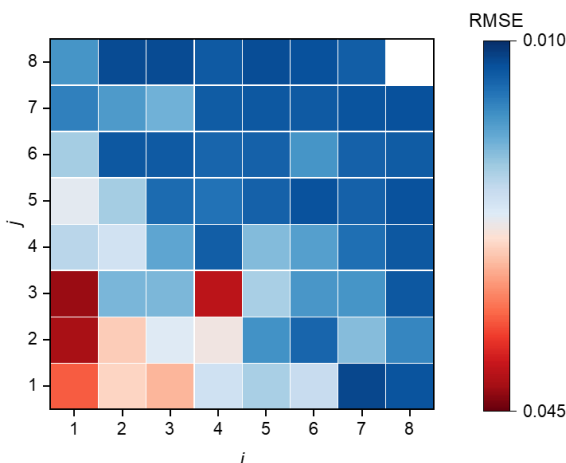
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Figure 2 Extracted features from the voltage relaxation curves as a function of battery capacity for NCA cells. (a) Variance (Var), (b) skewness (Ske), (c) maxima (Max), (d) minima (Min), (e) mean (Mean), and (f) excess kurtosis (Kur). Feature changes between 3500 mAh and 2500 mAh (71% of nominal capacity) for NCA cells are shown to be consistent with the used datasets. The mathematical description of the six features is depicted in Supplementary Table 5.



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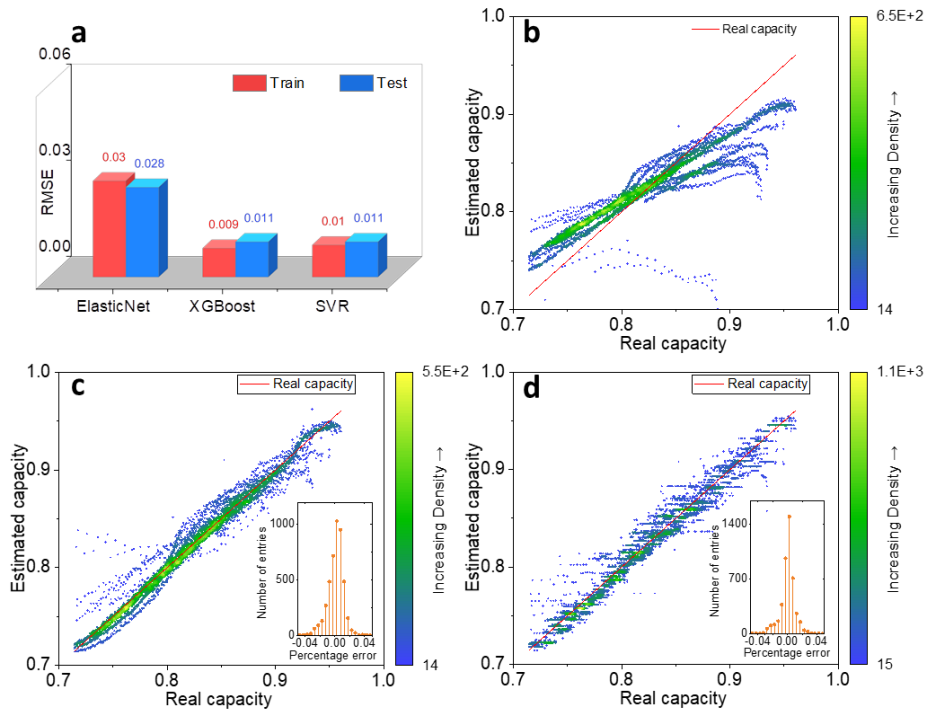
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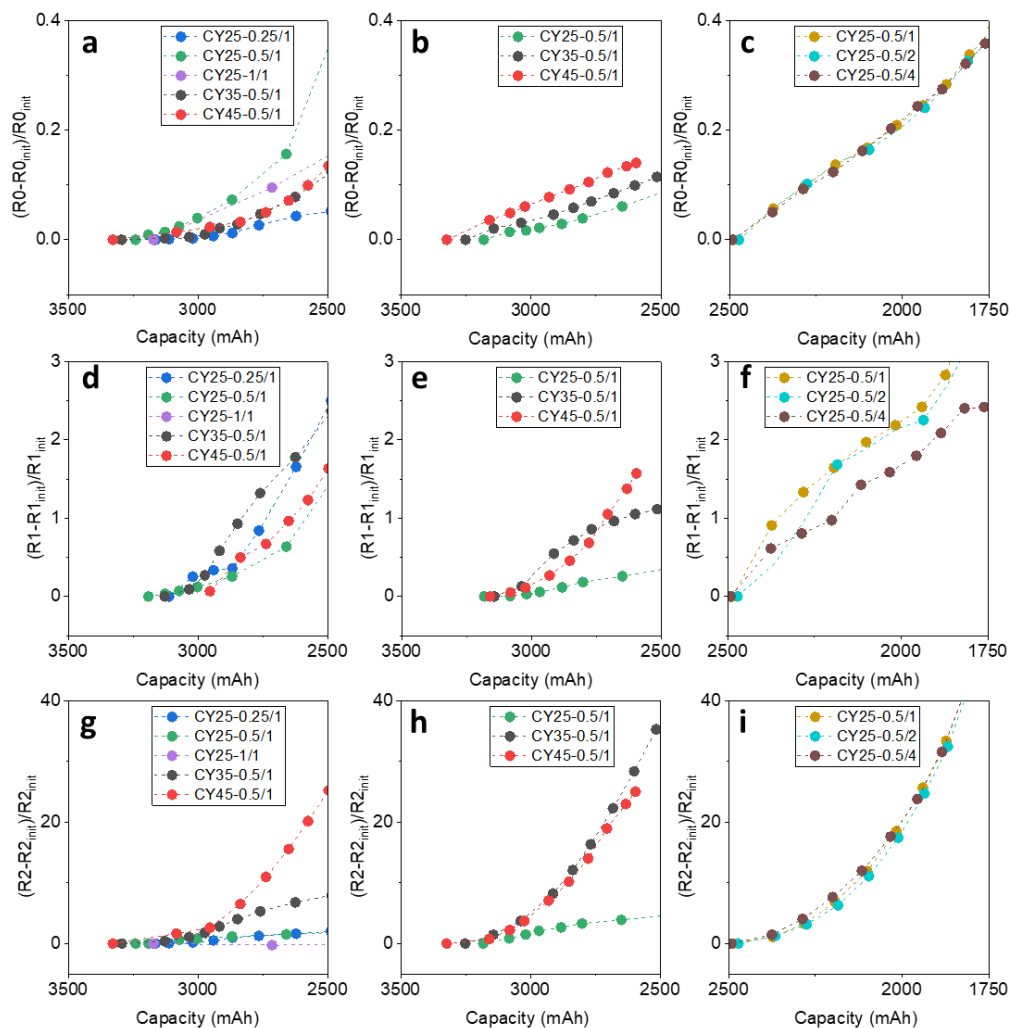
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Figure 3 Cross-validation root-mean-square error (RMSE) of the XGBoost method using different feature combinations. (i, j) means different feature combinations referring the Supplementary Table 10. The $(7, 1) = [\text{Var}, \text{Ske}, \text{Max}]$ obtains the best cross-validation RMSE = 1.0% within a three feature combination.



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Figure 4 Results of battery capacity estimation with the input of three features [Var, Ske, Max] by different estimation methods. The capacity results are uniformized by the nominal capacity for comparison. root-mean-square error (RMSE) of battery capacity estimation (a), test results of estimated capacity versus real capacity by ElasticNet (b), XGBoost (c), and Support Vectors Regression (SVR) (d)



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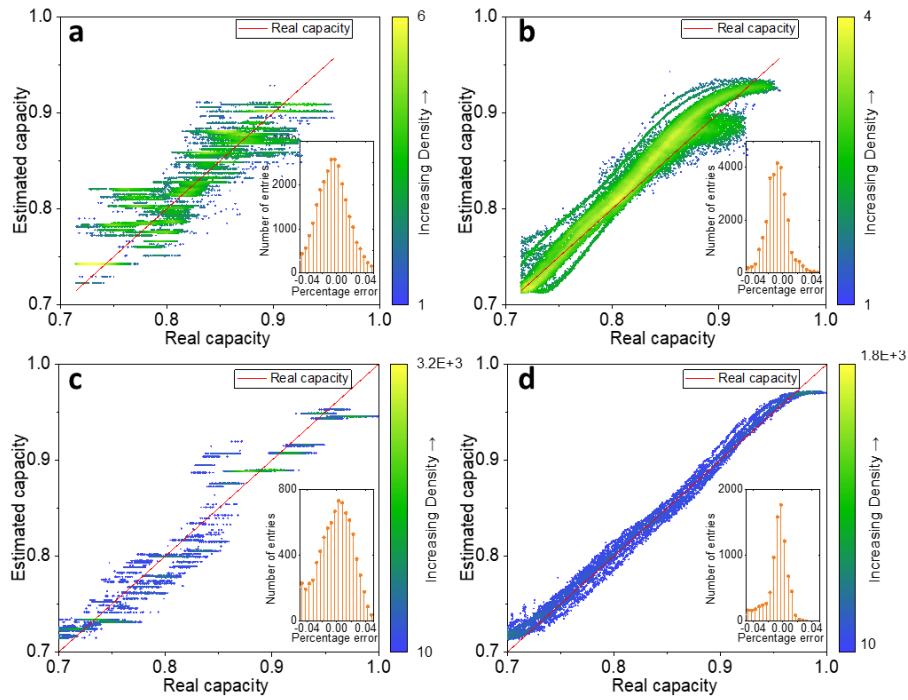
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Figure 5 AC electrochemical impedance variations of the lithium-ion cells during cycling. The resistance increment from the initial value (R_{init}) is calculated for comparison. The ohmic resistance of NCA cells (a), NCM cells (b), and NCA+NCM cells (c). SEI resistance of NCA cells (d), NCM cells (e), and NCA+NCM cells (f). Charge transfer resistance of NCA cells (g), NCM cells (h), and NCA+NCM cells (i). Only resistances before the capacity reducing to 71% of nominal capacity are shown to be consistent with the datasets in the study. The coefficient of determination (R^2) between the raw and fitted impedance data is summarized in Supplementary Table 12. The SEI resistances are not identified in some cycles (seen in Supplementary Table 12) for the NCA battery (d) and NCM battery (e). The shared information of raw impedance data and fitted data can be found in the data availability.



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Figure 6 Test results of estimated capacity versus real capacity by transfer learning. The capacity results are uniformized by the nominal capacity for comparison. Results of TL2 embedding XGBoost method (a) and embedding SVR (b) on dataset 2. Results of TL2 embedding XGBoost method (c) and embedding SVR (d) on dataset 3. Additional results are disclosed in Supplementary Figure 10-12.